

Challenges and Opportunities for Predicting Muons in Underground and Underwater Labs Using MUTE



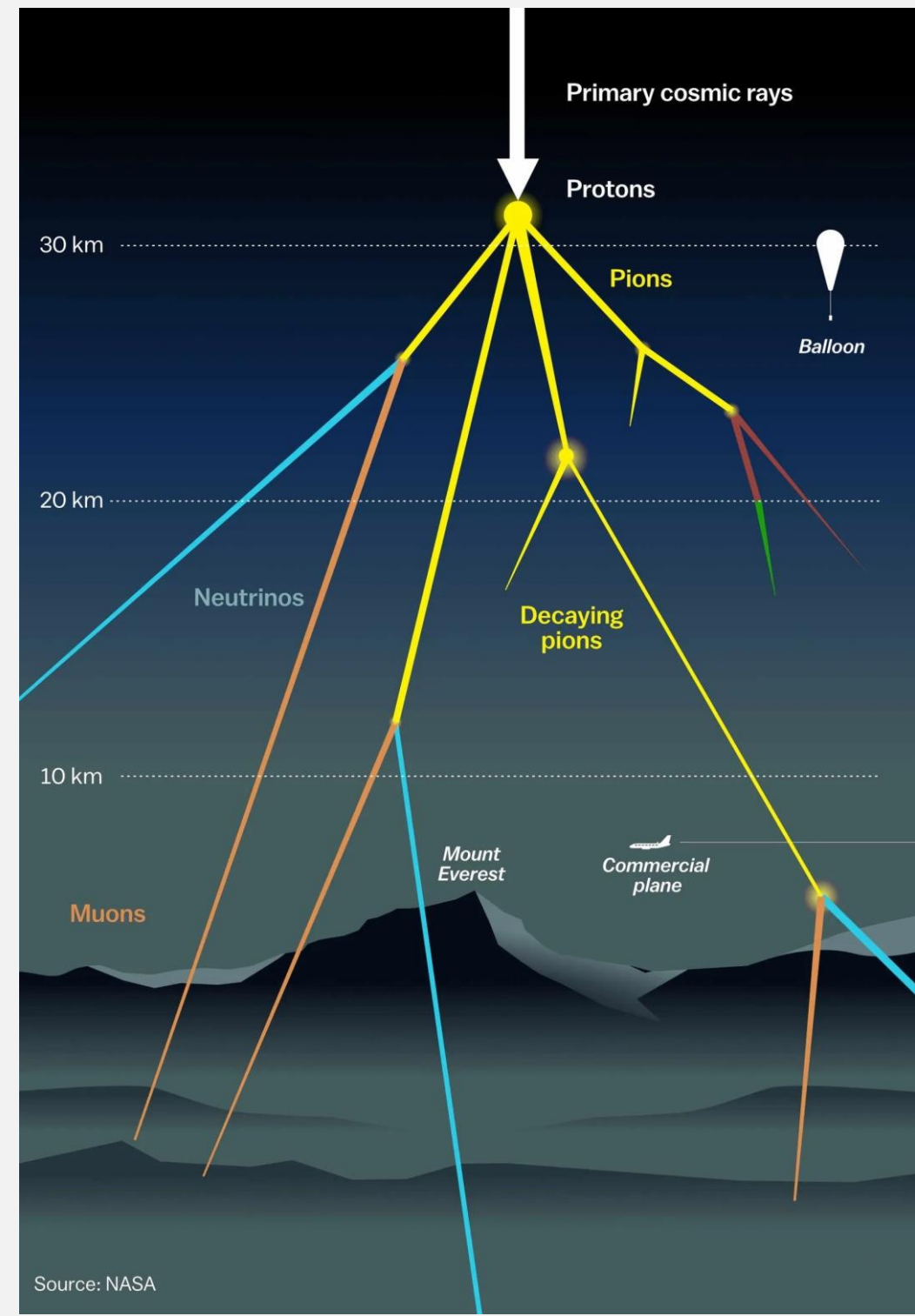
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INTRODUCTION

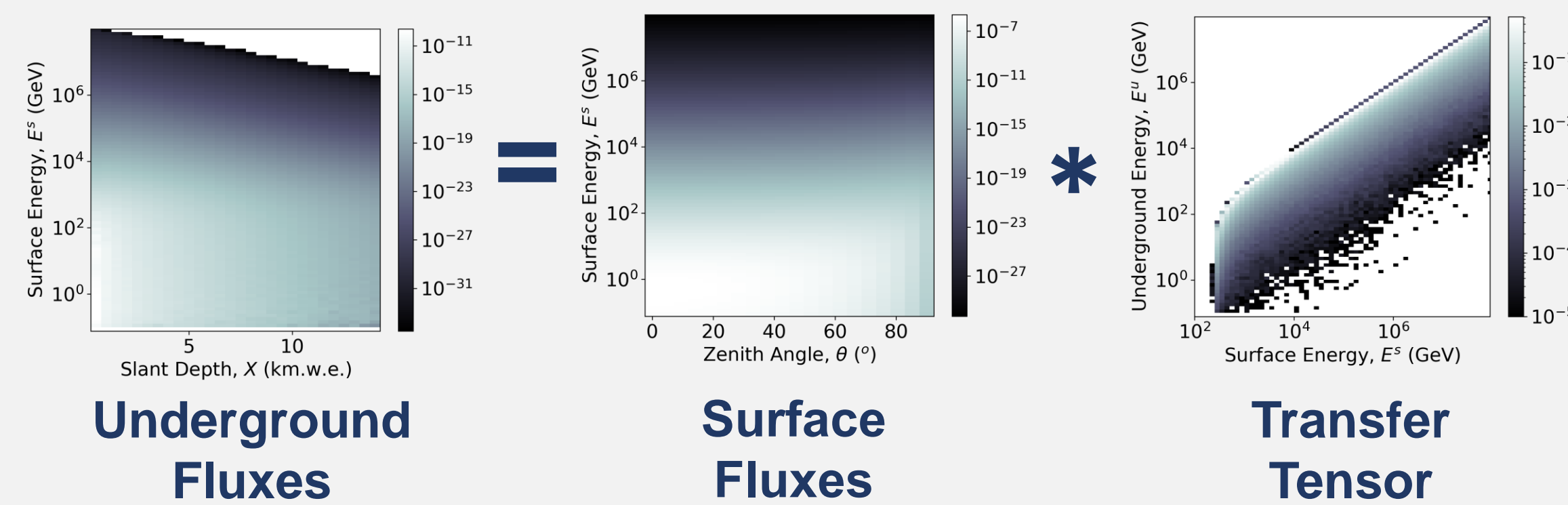
- Underground and underwater muons are crucial for data analyses in neutrino telescopes and in the design of Dark Matter detectors.
- MUTE** [1] is a computational tool released in 2021 that calculates atmospheric muon fluxes.
- We now introduce **MUTE v2** [2], which computes muon fluxes for labs under mountains.
- Our study employs the surface flux model **DAEMONFLUX** [3], which combines **DDM** [4] and Global Spline Fit [5].
- DAEMONFLUX** is calibrated to muon flux and ratio data and gives muon and neutrino flux uncertainties of <10% up to 1 TeV.



METHOD

- DAEMONFLUX** returns a surface flux matrix, and **PROPOSAL** [6] returns a surface-to-underground transfer tensor.
- Underground fluxes are calculated by the following convolution:

$$\Phi^u(E_j^u, X_k, \theta_k) = \sum_i \Phi^s(E_i^s, \theta_k) P(E_i^s, E_j^u, X_k) \left(\frac{\Delta E_i^s}{\Delta E_j^u} \right)$$



- The underground intensity is calculated by:

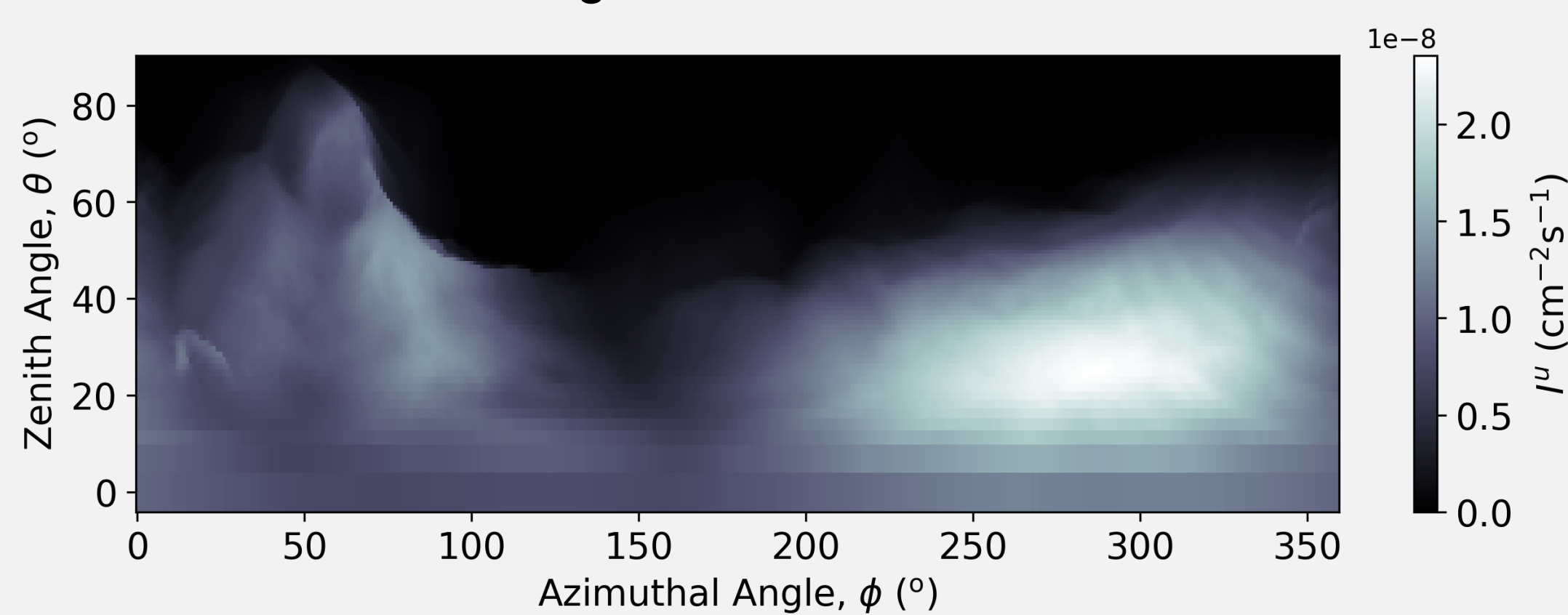
$$I^u(X, \theta) = \int_{E_{th}}^{\infty} \Phi^u(E^u, X, \theta) dE^u$$

- MUTE** can calculate intensities for both flat and non-flat overburdens.
- For labs under mountains, a grid of intensity values is calculated, and is then interpolated to the mountain profile read in from a geometry file.

$$\Phi_{tot}^u = \iint_{\Omega} I^u(X(\theta, \phi), \theta) d\Omega$$



- The result is a matrix of underground intensities as a function of zenith and azimuthal angle:



TOTAL FLUX

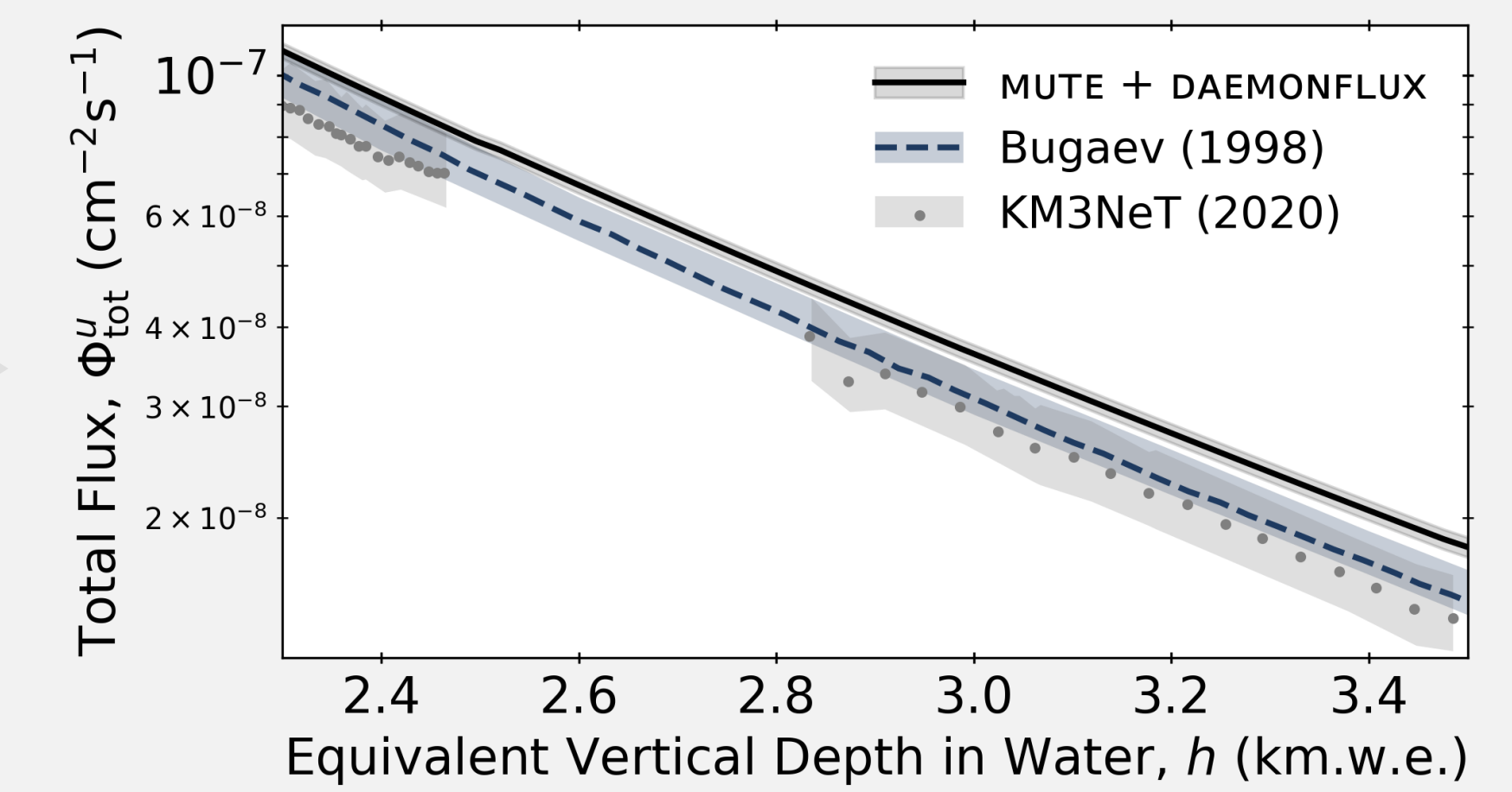
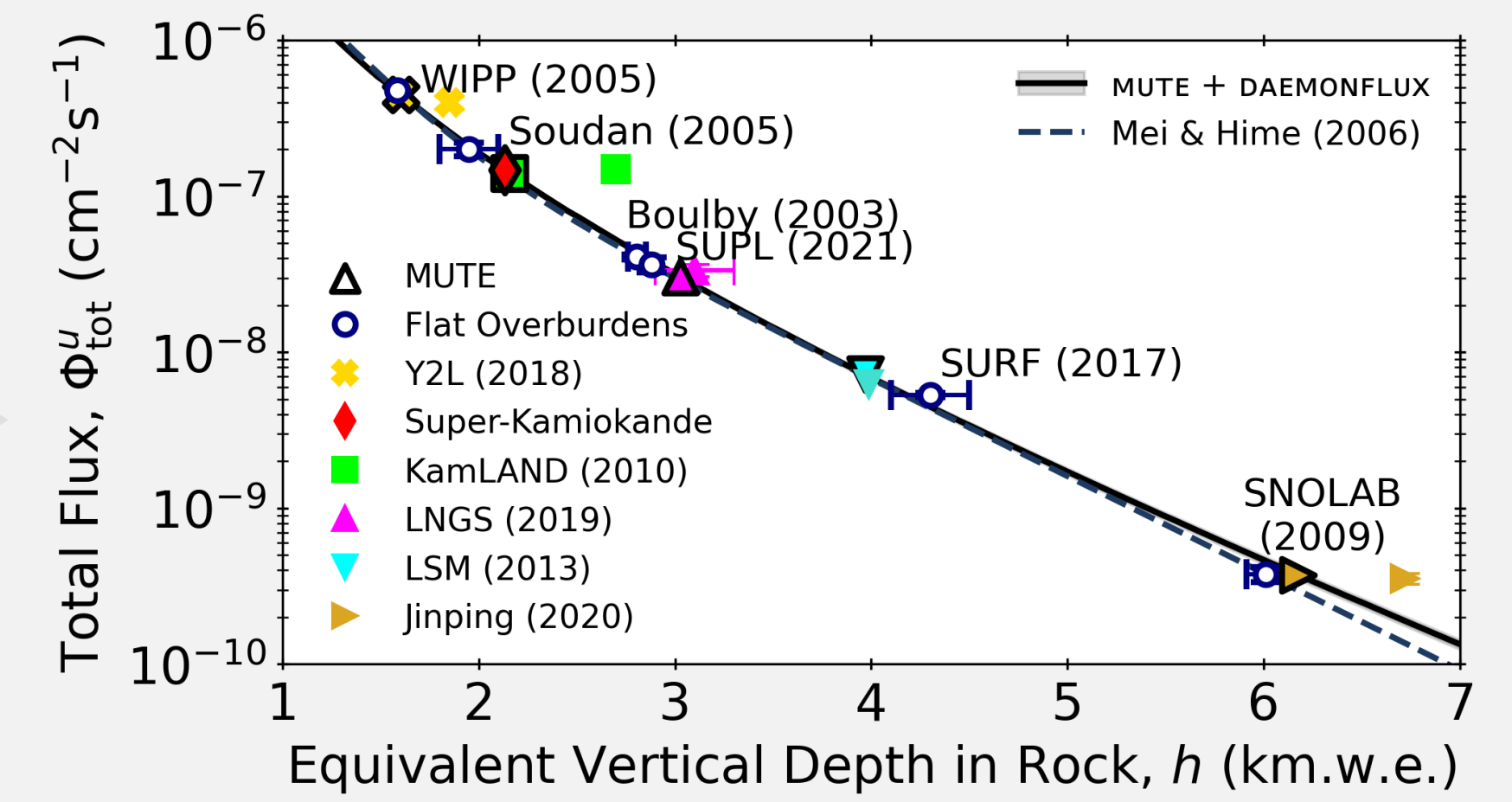
- The total muon flux is the main observable of interest for muon-induced backgrounds and has been calculated for labs underground and underwater with **DDM** and **DAEMONFLUX**.

Standard Rock

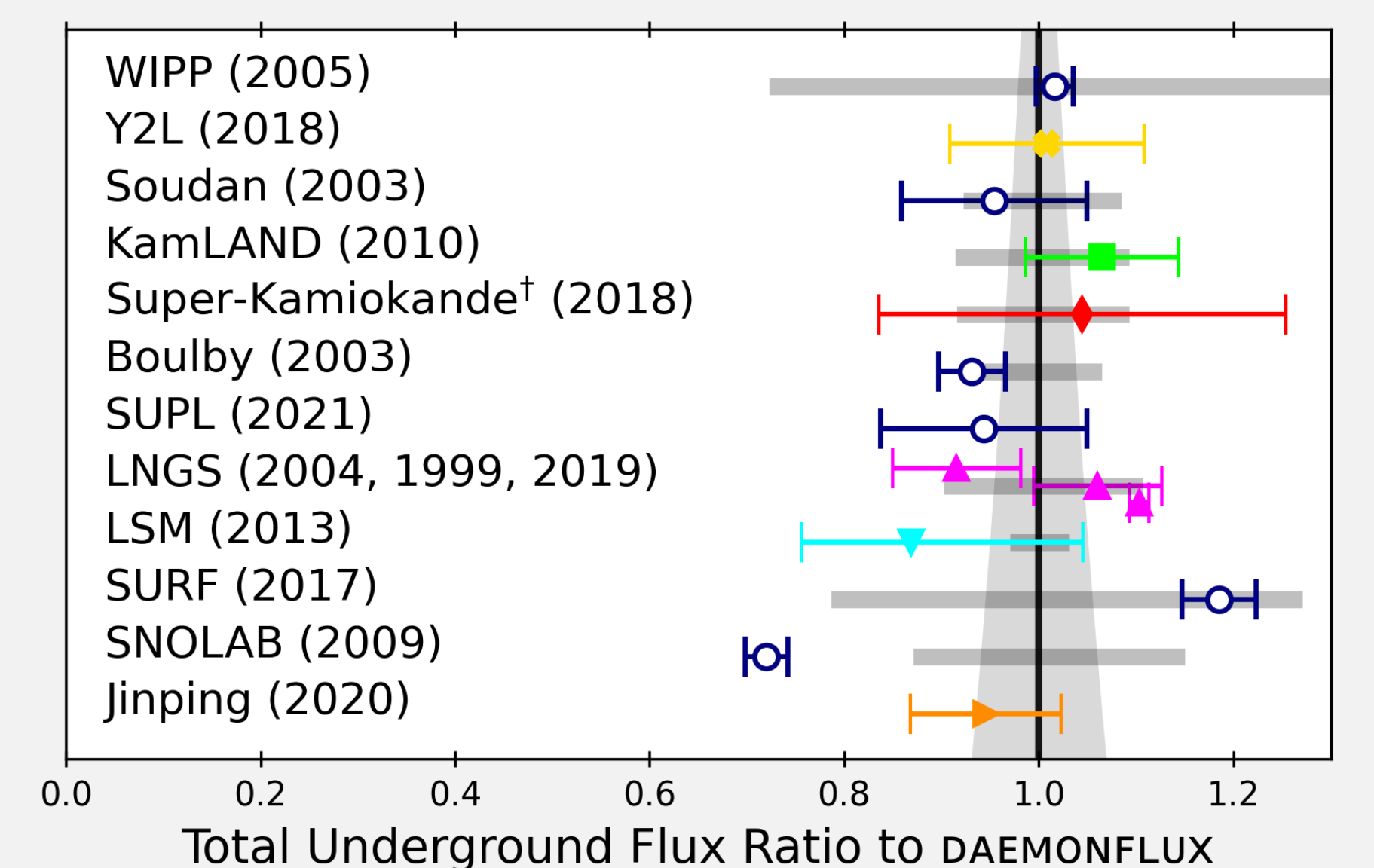
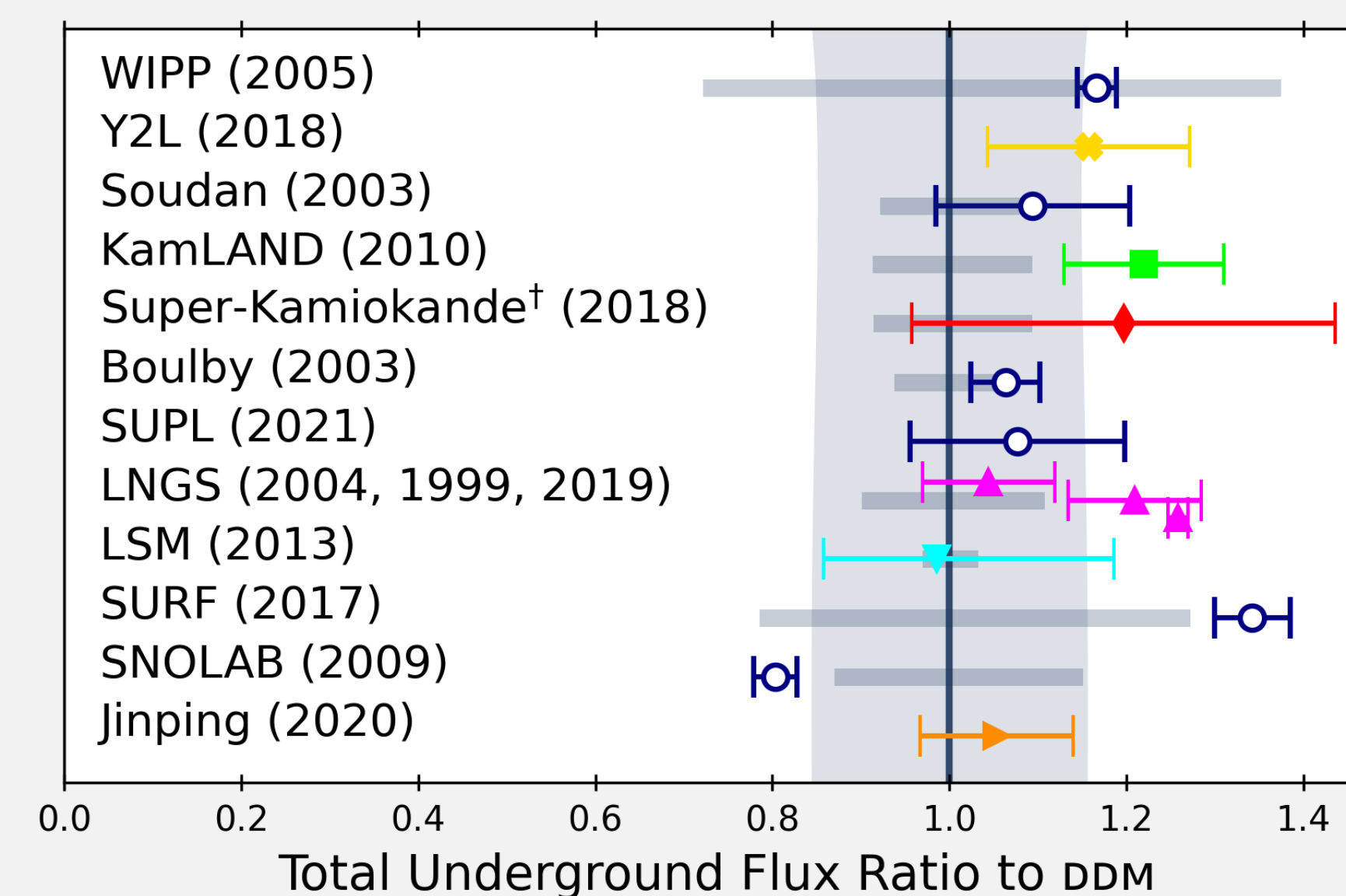
- We observe almost no systematic shift with **DAEMONFLUX**, compared to **DDM**, which has noticeably larger error bars and appears systematically lower than the data (see below).
- MUTE** with **DAEMONFLUX** provides a satisfactory description of the data, with the only exception being **SNOLAB**.

Water

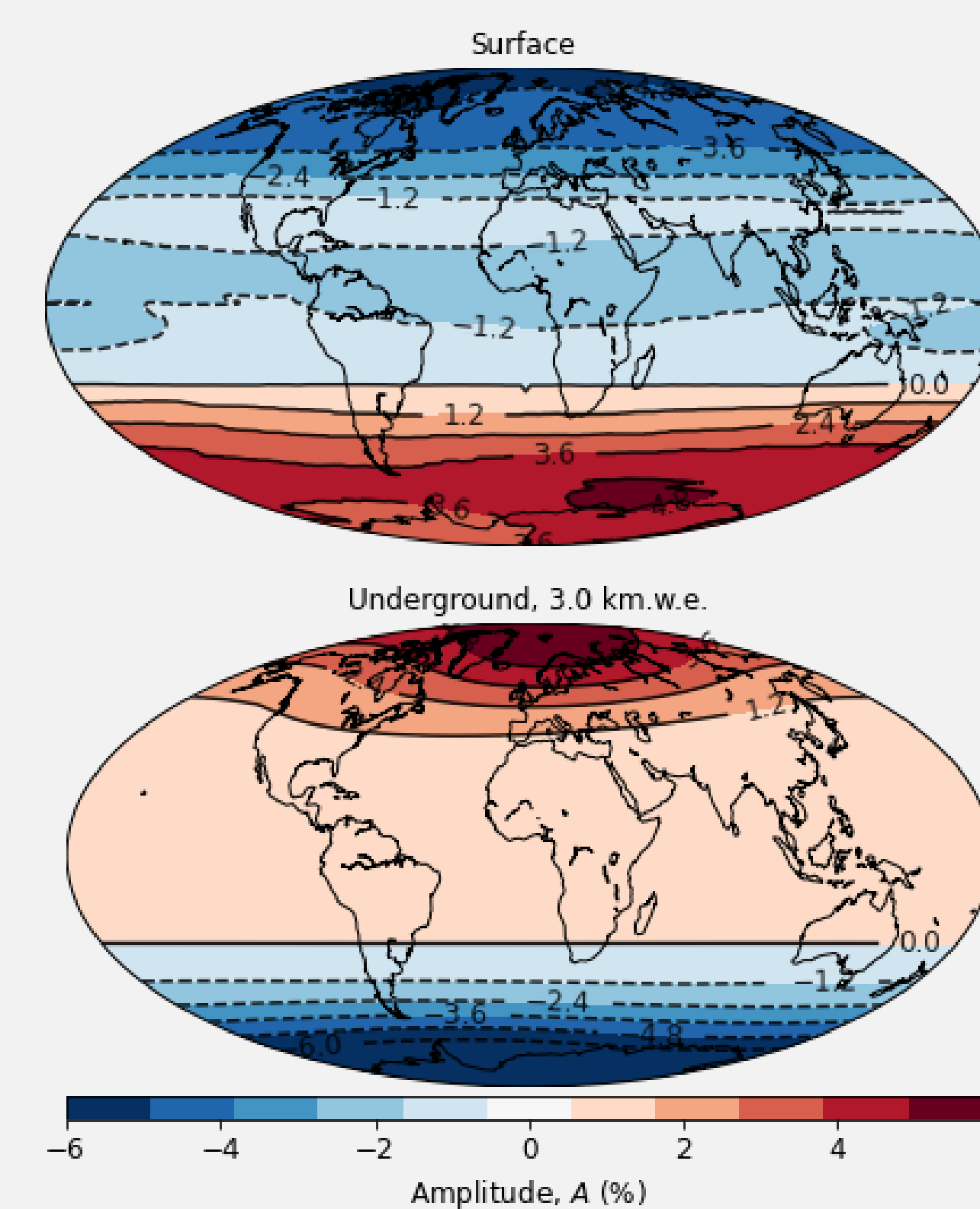
- We note that **KM3NeT** data is a factor of 2 below the prediction for water, but expect the level of precision of **MUTE** that we observe for rock to be applicable to water as well.



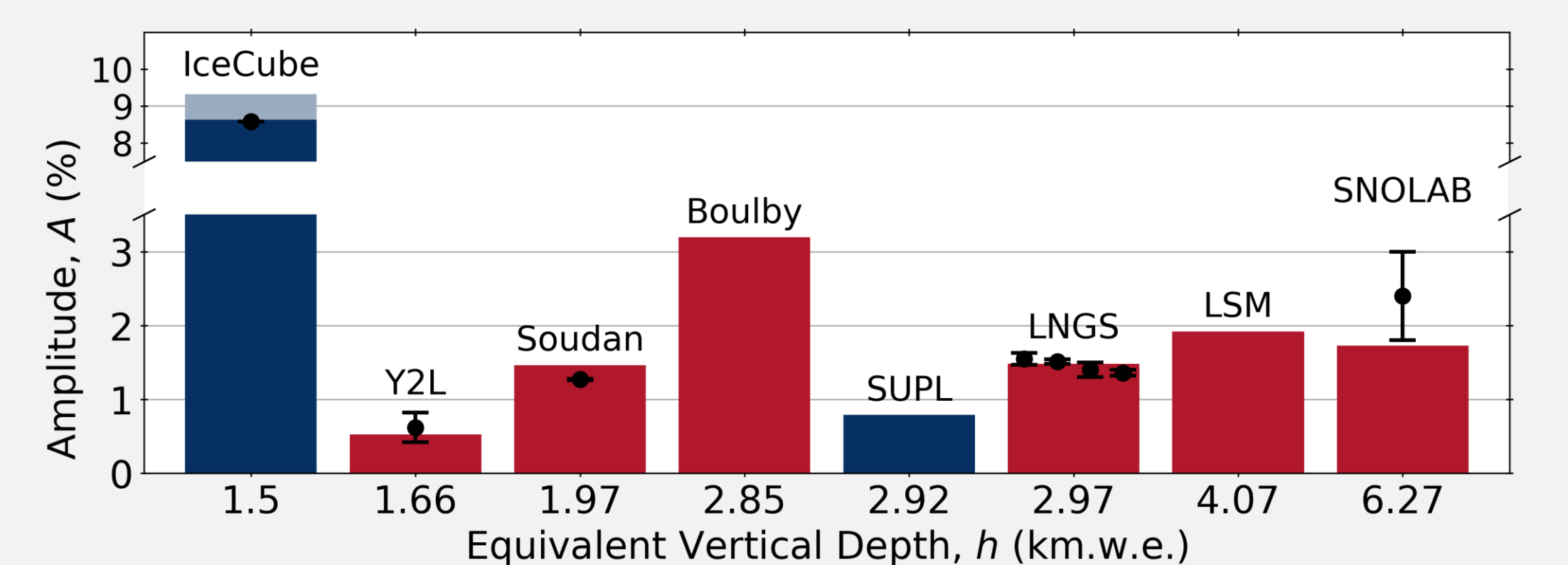
Ratios to Predictions for Standard Rock



SEASONAL VARIATIONS

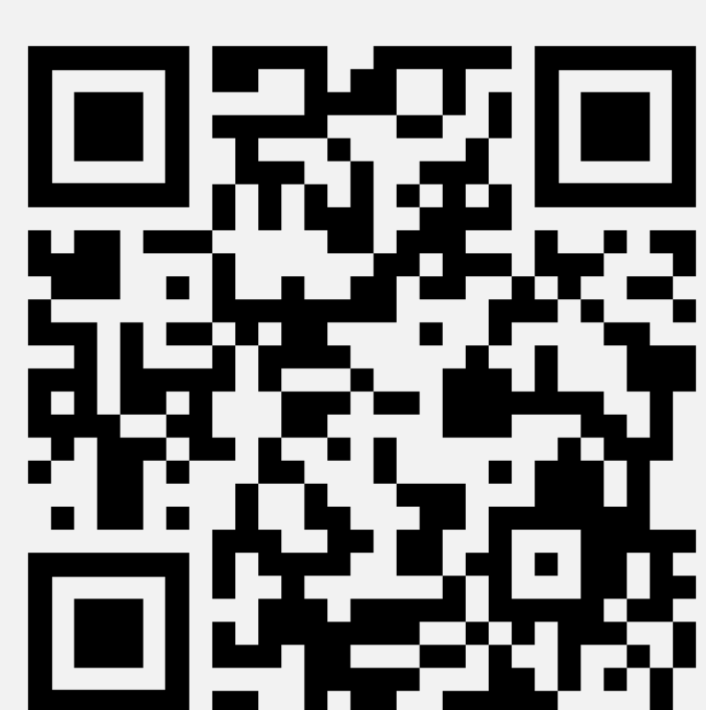


- The muon flux varies over the seasons due to changes to the temperature and density of the atmosphere.
- Energy-dependence of the decay and interaction processes means the sign of the amplitude of these variations inverts from surface to underground (see left).
- MUTE** calculates these amplitudes to high precision for labs in the **northern** and **southern** hemispheres (see below).



CONCLUSION

- MUTE** provides a **robust basis** for exploring underground muon flux data.
- We match total flux data for most locations within uncertainties for rock and await more data for water.
- We observe **good compatibility** with available data for amplitudes of seasonal variations.



MUTE can be installed via pip:

```
$ pip install mute
```

PROPOSAL will need to be installed in order to generate custom transfer tensors. Full installation instructions are given on the GitHub page: <https://github.com/wjwoodley/mute>.

References

- [1] A. Fedynitch, et al., *ApJ* **928** (2022) 27.
- [2] W. Woodley and A. Fedynitch, [10.5281/zenodo.5791812](https://arxiv.org/abs/10.5281/zenodo.5791812).
- [3] J. P. Yañez and A. Fedynitch, *PRD* **107** (2023) 123037.
- [4] A. Fedynitch and M. Huber, *PRD* **106** (2022) 083018.
- [5] H. P. Dembinski, et al., *PoS ICRC2017* (2018) 533.
- [6] J.-H. Koehne, et al., *CPC* **184** (2013) 2070.

Acknowledgements

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